Power modulation based optical fiber loop-sensor for structural health monitoring in composite materials

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SysInt 2014, Bremen, Germany

List of Publications and Patents

- The technologies covered in this work are presented in the following
 - Patents:
 - Fiber-optic extensometer, US Patent #8,428,400, April 23, 2013, Nikhil Gupta, Nguyen Q. Nguyen.
 - Method for measuring the deformation of a specimen using a fiber optic extensometer, US Patent #8,649,638, February 11, 2014, Nikhil Gupta, Nguyen Q. Nguyen.
 - Papers:
 - Nishino, Z., Chen, K., and Gupta, N. Power Modulation Based Optical Sensor for High Sensitivity Vibration Measurements. IEEE Sensors, 2014, (7): p. 2153 2158.
 - Nguyen, N. Q. and Gupta, N. Whispering gallery mode sensor for phase transformation and solidification studies. Philosophical Magazine Letters, 2010. 90(1): p. 61-67.
 - Nguyen, N. Q. and Gupta, N., Analysis of an encapsulated whispering gallery mode micro-optical sensor. Applied Physics B: Lasers and Optics, 2009. 96(4): p. 793-801.
 - Nguyen, N. Q. and Gupta, N., Power modulation based fiber-optic loop-sensor having a dual measurement range. Journal of Applied Physics, 2009. 106(3), #033502.

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Introduction

- Structural Health Monitoring (SHM) A process of identifying one or more of
 - Load applied or displacement obtained on the structure
 - Extent of damage
 - Growth rate of damage
 - Performance of the structure as damage accumulates
- SHM can help in moving from *predictive maintenance* to *need-based maintenance*

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- Increase in safety
- Cost saving



Whispering Gallery Mode Sensors



- Tunable laser is used
- Evanescent field of the stripped off section of fiber interacts with that of the resonator (particle)
- Coupling back of the evanescent field in the fiber gives resonance peaks, which can be tracked







Whispering Gallery Mode Sensors

- Very high sensitivity
 - Detection of single chemical molecules
 - Detection of a single HIV virus
 - Measurement of subnanometer displacement
 - For $r >> \lambda$, resonance condition:

$$2\pi r n \approx \ell \lambda$$
 ($\ell = integer$)

$$\frac{\Delta n}{n} + \frac{\Delta r}{r} \approx \frac{\Delta \lambda}{\lambda}$$



- n = refractive index of the microsphere
- λ = wavelength
- r = micro-sphere radius





WGM Sensors: Effect of **Refractive Index**

$$n_{1} = n_{0} + C_{1}\sigma_{1} + C_{2}(\sigma_{2} + \sigma_{3})$$
$$n_{2} = n_{0} + C_{1}\sigma_{2} + C_{2}(\sigma_{1} + \sigma_{3})$$

$$n_3 = n_0 + C_1 \sigma_3 + C_2 \left(\sigma_1 + \sigma_2\right)$$

Where

 n_0 undeformed index of refraction

 σ_1 , σ_2 and σ_3 are principal stresses

 C_1 and C_2 are elasto-optic coefficients of the material of the sphere.

- Sensitivity comes at a price!
 - Signal to noise ratio can be low
 - Keeping the particle in resonance can be difficult

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	Silica (Yves Belouard et al. 2006)	PMMA (Feridun et al. 2004)
C ₁ (m ² /N)	-4.22 x10 ⁻¹²	-12 x10 ⁻¹²
<i>C</i> ₂ (m ² /N)	-0.65 x10 ⁻¹²	-12 x10 ⁻¹²
n ₀	1.467	1.4876



Introduction







- Microbend sensors
 - Use multi-mode fiber
 - Require high power light source
 - Normally used under compression
 - Large size



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Micro and Nano Composites

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Results and Discussion

- Power attenuation
- Critical radius (Jeunhomme, 1983) where
 - λ is the operating wavelength λ_c is cut-off wavelength Δn : core-cladding index of refraction difference
 - For present single-mode optical fiber
 - λ =1.31 μm, λ_c =1.26 μm, Δn =0.0058

R_c=11.8 mm



$$R_{c} = 20 \frac{\lambda}{\left(\Delta n\right)^{3/2}} \left(2.748 - 0.996 \frac{\lambda}{\lambda_{c}}\right)^{-2}$$



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• Power transmission due to curvature

$$\overline{P}_R = \frac{P_{out}}{P_{in}}$$

*P*_{out} is transmitted power through the loop *P*_{out} is power incoming to the loop

• Compressing loop creates more losses, relative transmitted power

$$\overline{P} = \frac{P'_{out}}{P}$$

- P'_{out} is transmitted power with the applied force





 $- P_{out}$ is power with no load applied



Composite Materials & Mechanics Laboratory Innovation in Micro and Nano Composit



• Compression of loop $R_B = 7 \text{ mm}$



- + R
- coating cladding eore R_B

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• Resonances occur between leaky mode reflected from cladding/coating interface and fundamental mode

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• Pure bend loss-Marcuse model

Assumption: infinite cladding, large bend radius, weakly guided index fiber

$$\overline{P}_{R} = \exp\left(-2\alpha_{B}l_{B}^{e}\right)$$
where
$$k = V = V$$

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 $k = 2\pi / \lambda$ $V = ak \left(n_{co}^{2} - n_{cl}^{2} \right)^{1/2} \quad l_{B}^{e}$ $\kappa = \left(k^{2} n_{co}^{2} - \beta_{0}^{2} \right)^{1/2}$ $\gamma = \left(\beta_{0} - k^{2} n_{cl}^{2} \right)^{1/2}$

SMF28e from Corning, NY

Fiber layer	Radius (µm)	Index of refraction
Core	4.1	1.4517
Cladding	62.5	1.447
Coating	125	1.4786

$$2\alpha_B = \frac{1}{2} \left(\frac{\pi}{\gamma^3 R_B^e}\right)^{1/2} \frac{\kappa^2}{V^2 K_1^2 (\gamma a)} \exp\left(-\frac{2\gamma^3 R_B^e}{3\beta_0^2}\right)$$
$$\frac{e}{R_B^e} = 2\pi R_B^e$$

 n_{co} and n_{cl} are indices of refraction of the core and cladding

 β_o is the propagation constant in straight fiber, solved by the eigenvalue equation

$$\kappa \frac{J_1(\kappa a)}{J_0(\kappa a)} = i\gamma \frac{H_1^1(i\gamma a)}{H_0^1(i\gamma a)}$$

 R^{e}_{B} is effective bend radius, differing from R_{B} by a stress correction factor, taken 1.28 for SMF28e fiber





• Renner model- finite, coating and cladding thickness

 $\overline{P}_R = \exp\left(-2\alpha_{BC}l_B^e\right)$

where

$$2\alpha_{BC} = 2\alpha_{B} \frac{2(Z_{ct}Z_{cl})^{1/2}}{(Z_{ct} + Z_{cl}) - (Z_{ct} - Z_{cl})\cos(2\Theta_{0})}$$
$$Z_{cl} = k^{2}n_{cl}^{2}(1 + 2b/R_{B}^{e}) - \beta_{0}^{2}$$
$$Z_{ct} = k^{2}n_{ct}^{2}(1 + 2b/R_{B}^{e}) - \beta_{0}^{2}$$
$$\Theta_{0} = \frac{\gamma^{3}R_{B}^{e}}{3k^{2}n_{cl}^{2}} \left(\frac{R_{c}}{R_{P}^{e}} - 1\right)^{3/2} \qquad R_{c} = \frac{2k^{2}n_{cl}^{2}b}{N^{2}}$$

 $\frac{4b\gamma R_B^e}{3\pi R_c} \left(\frac{R_c}{R_B^e} - 1\right)^{3/2} = \begin{cases} 2m - 1/2 \text{ for maximum} \\ 2m - 3/2 \text{ for minimum} \end{cases}, m$

, *m* is an integer

- $l_B^e = 2\pi R_B^e$ is the effective length of the loop R_c is the critical radius
- Experimental data are obtained by changing the radius of
 fiber-loop



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Loop sensor calibration setup

- Square wave signal is sent to the loop
- Photodetector tracks the transmitted power
- Relative transmitted power and force are monitored with respect to increment in displacement





Loop sensor calibration

• Calibration of different loop radii



- Smaller loops have higher sensitivity but lower measurement range
- Loop-sensors allow large deformation without losing its elasticity and repeatability

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Loop sensor calibration







Cyclic loading tests

• Pear-shaped loop and experimental setup



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Cyclic loading tests

• Results in 10,000 cyclic loading





- Loop radius: 5 mm
- Displacement: 6 mm

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- Displacement rate: 0.4 mm/s
- 30 s per loading/unloading cycle

- Total testing time: 4 days
- The sensors survived after 10,000 cycles
- Results show repeatability and consistency for 10⁴ loading/unloading cycles



Cyclic loading tests

• Different displacement rate

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- Loop radius: 6 mm
- Displacement: 6 mm





SHM of laminated composites

• Loop sensors bonded to laminated composites under flexural loading



SHM of laminated composites





Quasi-static loading on loop of radius 6 mm







Vibration Measurement



Optical fiber loop sensor setup for calibration of vibration measurement

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The setup used for measuring the free vibration characteristics of a composite material.





Vibration Measurement



- The Vibration measurements are accurate and match with the frequency of the shaker
- No fatigue or hysteresis is observed for over 10,000 cycles

Results and Discussion



- The system is tested with and without optical fiber sensor using only a PSD
- Then the output of the sensor is related to the PSD measurements

Conclusions

- A low-cost, high sensitivity loop-sensor has been developed for stress or strain measurement
- The sensor can be used in dual measurement ranges for displacement
- The sensor shows survivability in large number of loading cycles
- Use of loop-sensor for vibration measurement is possible
- Potential applications in chemical sensing



Acknowledgements

- National Science Foundation grant # CBET 0809240/0619193
- Environmental Protection Agency: Smart Fellowship to Kevin Chen for chemical sensing
- Zachary Nishino, Dr. Nguyen Q. Nguyen
- Dr. Volkan Otugen's group at Southern Methodist University, Dallas

